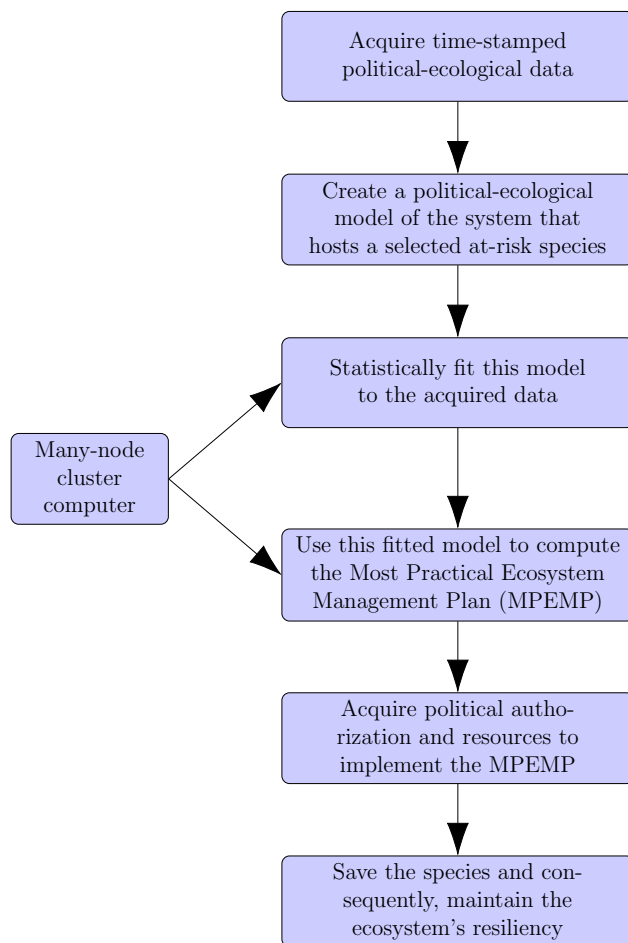


Graphical Abstract

Using Political-Ecological Models to Sustain Biodiversity



Highlights

Using Political-Ecological Models to Sustain Biodiversity

- A new toolkit finds politically feasible and effective ecosystem management plans.
- A new cluster computing optimization algorithm is described.
- This algorithm permits the computation of these ecosystem management plans.
- Statistical estimation of political-ecological model parameters also become possible.
- A new model captures the East African cheetah-hosting political-ecological system.

Using Political-Ecological Models to Sustain Biodiversity

Abstract

Because of the finality of a species' global extinction, there is a need to focus on stopping such extinction events from happening. The way forward is to find and implement politically feasible and ecologically effective projects that head off extinction events. This article delivers a software toolkit that implements one way to do this. This toolkit provides an organization the means to (1) build a political-ecological model; (2) fit this model to a political-ecological data set; and finally, (3) use this model to compute the *most practical ecosystem management plan* (MPEMP). This model-based approach to first understanding the political issues surrounding the conservation of a particular species and then second, finding a conservation plan that works with these political realities – is hamstrung by the expensive computations needed to first, fit a political-ecological model to data and then second, compute the MPEMP from this fitted model. Therefore, a new optimization algorithm is presented that overcomes this challenge when run on either a commercial or home-grown cluster computer. This new algorithm finds the global solution to an optimization problem characterized by constraints and a black-box, stochastic objective function. This toolkit is illustrated by finding the MPEMP for conserving the cheetah (*Acinonyx jubatus*) population across Kenya and Tanzania.

Keywords: extinction crisis, biodiversity conservation, political-ecological models, model credibility, ecosystem management, robust statistical estimators, optimization algorithms, high performance computing

1 Abbreviations:

- 2 CA: Consistency Analysis
- 3 IBM: Individual Based Model
- 4 MDAS: Multiple Dimensions Ahead Search
- 5 MPEMP: Most Practical Ecosystem Management Plan

6 NGO: Nongovernmental Organization
7 PACSA: Parallel Asynchronous Coupled Simulated Annealing
8 SA: Simulated Annealing
9 SA-MDAS: Simulated Annealing – Multiple Dimensions Ahead Search
10 SDE: Stochastic Differential Equation
11 TSCC: Triton Shared Computing Cluster

12 1. Introduction

13 Earth is in the midst of an extinction crisis (Torres-Romero et al., 2024),
14 (Garber et al., 2024) with many species becoming globally extinct every year
15 (Verones et al., 2022). Global extinction of a species is irreversible. Assuming
16 that the end goal of environmental and ecological conservation efforts is to
17 sustain ecosystems in states that are close to those circa 2025, it can be argued
18 that conservation efforts that directly contribute to stemming irreversible
19 ecosystem state changes should be given the highest priority both politically
20 and financially. To support these efforts, this article argues that the highest
21 priority should be given to (a) developing *political-ecological* models that can
22 credibly gauge likelihoods of global extinction events; and (b) developing
23 ecosystem management plans based on these models that can reduce these
24 likelihoods.

25 This article argues that *biodiversity conservation* efforts in particular,
26 should focus on understanding the political-ecological processes that lead to
27 global extinction events so that politically feasible and ecologically effective
28 ecosystem management plans can be identified that, when implemented, have
29 the greatest chance of stopping these events from happening.

30 This article describes a free software toolkit for developing such plans.
31 Armed with this toolkit, an organization first statistically estimates the pa-
32 rameter values of a political-ecological model. They then use this fitted model
33 to compute the *most practical ecosystem management plan* (MPEMP) (Haas,
34 2011, Chapter 4). Accordingly, this toolkit is referred to here as the *MPEMP*
35 *constructor*.

36 This article takes a broad view of what constitutes biodiversity to include
37 species that may not have any commercial value but are listed as Vulnerable
38 or Endangered on the IUCN Red List (Panwar et al., 2023), (Testa et al.,

2025), (Tobias et al., 2025). Such species include many terrestrial mammals,
marine mammals, fish, and many plants.

The private sector, although paying lip service to the conservation of such
species, actually has a strong economic interest in biodiversity conservation
that is focused mainly on the preservation of potentially profitable genetic re-
sources. The commercial value of these resources was approximately USD44
trillion in 2022 (Medlong et al., 2022). The total budget of NGOs engaged
in preserving endangered species by comparison, is in the neighborhood of
USD12 billion (Wan, 2023). The efforts of the many professionals engaged in
work to curb biodiversity loss, although laudable, is dwarfed by the efforts in
the private sector to profit from biodiversity resources. In other words, the
big money is being spent on preserving species that have high commercial
potential rather than on species that, in-part, define the word, “wild.”

Some efforts are being made, however, to encourage more private sector
spending on species who have no commercial value but do have (1) *existence*
value, (2) *bequest value*, or (3) *ecosystem function value*, i.e., the species
performs important ecosystem-support functions. Existence value is the per-
ceived value of knowing that a species exists, and bequest value is the per-
ceived value of conserving a species for future generations (Ressurreição et
al., 2012).

Beverdam et al. (2025) for example, call for a “blending” of private and
public sector funds to conserve species that are not commercially valuable.
An example of this type of financing mentioned by these authors is the so-
called “Rhino Bond” that targets the conservation of the commercially val-
ueless black rhinoceros (*Diceros bicornis*) in Africa.

1.1. The way forward

The concept that this article is offering a realization of, is a toolkit that
can find conservation plans that are ecologically effective and politically fea-
sible to implement. After describing how this concept is realized in software,
this article gives a proof of this concept by finding a management plan for the
East African cheetah that requires minimal changes to the political beliefs of
those groups surrounding this biodiversity conservation challenge while pre-
dicting that the cheetah population will remain viable through the planning
horizon.

73 As an example of this article’s approach to biodiversity conservation, Haas
74 and Ferreira (2017) build an agent/individual based model of the political-
75 ecological system that surrounds rhinoceros (*Ceratotherium simum*) poaching
76 in South Africa. These authors simulate several management options and
77 predict that under current management policies, rhinos in South Africa will
78 become extinct around the year 2036.

79 Such models, however, are in their infancy but need to quickly mature be-
80 cause at present extinction rates, many species including most large mammals
81 will be globally extinct by about 2055 (Ceballos et al. , 2015). In other words,
82 if present trends continue, a significant proportion of the earth’s species will
83 soon be gone due mainly to the activities of the most recent (circa 2025)
84 several generations of humans.

85 This article gives a tested toolkit, namely, the MPEMP constructor that
86 can be used to (a) model such political-ecological systems; and (b) based
87 on such models, compute ecosystem management plans that, when imple-
88 mented, fend off species extinction events. The MPEMP constructor stream-
89 lines the construction of an integrated model composed of agent-based sub-
90 models of political processes that interact with an individual-based popula-
91 tion dynamics submodel of an at-risk species.

92 What mechanisms of biodiversity loss would such models represent? Habi-
93 tat loss is often pointed to as the principal driver of global biodiversity loss
94 (Hanski, 2011). But recently, one study could find no statistical difference
95 between loss of habitat and *direct exploitation*, i.e., intentional harvesting
96 of wildlife either legally or illegally (Jaureguiberry et al., 2022). Illegal har-
97 vesting and illegal trading of wildlife is referred to as *wildlife trafficking*.
98 The scale of exploitation-curbing biodiversity conservation projects that is
99 needed to slow the globe’s ongoing biodiversity losses, is much larger than
100 the sum total of currently active projects. To help address this disparity,
101 the MPEMP constructor is engineered to focus on the modeling of direct
102 exploitation drivers of biodiversity loss.

103 Recently, the literature has called for a more holistic view of biodiversity
104 conservation rather than a focus on single species preservation (Tobias et al.,
105 2025). This view, called “process-based” by Tobias et al. (2025) argues that
106 maintaining ecological processes that drive critical ecosystem functioning,

107 should be the primary goal of biodiversity conservation initiatives. These
108 processes include adaptation, gene flow, dispersal, and trophic interactions.

109 Acknowledging that the goal of avoiding the extinction of species that
110 have evolved over millions of years is not to be abandoned, Tobias et al.
111 (2025) call for a synthesis of species-centric and process-based approaches to
112 biodiversity conservation:

113 “We advocate integration and communication across the two pri-
114 mary cultures of conservation—species-centric and process-based—as
115 the most effective progress will occur when these two missions op-
116 erate in tandem and synergistically ((Tobias et al., 2025)).”

117 Process-based approaches to biodiversity conservation, however, have yet to
118 wrestle with direct exploitation effects on an ecosystem’s functioning.

119 Such integration is straightforward within the methods detailed in this
120 article. For instance, *functional diversity* (FD) is one way to describe the
121 healthy functioning of an ecosystem. FD can be quantified from remotely-
122 sensed NDVI data (Li et al., 2025). And, *trophic transfer* between predators
123 and their prey can be quantified with the *AB ratio* reviewed in Carroll et al.
124 (2019). These two metrics can easily be added to the species abundance ob-
125 jective function employed in this article to arrive at an analysis and planning
126 workflow that integrates species-centric goals and process-based goals.

127 The MPEMP maximally increases the probability of a species’ survival
128 while requiring the least change in the beliefs held by identifiable groups
129 of humans in those countries that host a selected at-risk species. Indeed,
130 according to Haas (2024c), any project that is intended to sustain biodiversity
131 needs to have its MPEMP computed so that the conservation project can
132 either be modified to enhance its conservation effectiveness – or abandoned
133 altogether and replaced by a project that implements the MPEMP. The
134 MPEMP constructor guides the user through this MPEMP computation.

135 An organization would use the MPEMP constructor to complete the fol-
136 lowing five steps.

- 137 1. Acquire a data set that pertains to the political-ecological system sur-
138 rounding a selected at-risk species.
- 139 2. Create a political-ecological model of this system.

- 140 3. Compute statistical estimates of this model's parameters.
- 141 4. Display and assess the political-ecological actions generated by this
- 142 fitted model.
- 143 5. Compute the MPEMP from this fitted model and implement it.

144 This five-step procedure has application in a business-oriented approach to
 145 conserving a selected at-risk species (Haas, 2022), (Haas, 2024c). Briefly,
 146 revenue from a commercial *offering* funds a *biodiversity project*. This project
 147 operationalizes the MPEMP that has been computed for that species and
 148 the political-ecological system that hosts it.

149 This article proceeds as follows. A description is given in Section 2 of
 150 this *interacting influence diagrams* modelling architecture (Haas, 2011, Chap-
 151 ter 2). Then, as an example, this architecture is used to build a model of
 152 the political-ecological system that hosts the East African cheetah (*Acinonyx*
 153 *jubatus*) population. A new cluster computer-based optimization algorithm
 154 is presented in Section 3 that has developed out of proposals advanced by
 155 Haas (2024). The above model is fitted via this new algorithm to a *political-*
 156 *ecological actions history* data set in Section 4. Statistical estimates of this
 157 model's parameter values found via Consistency Analysis (CA) (Haas, 2011,
 158 Chapter 3) are computed by running the new optimization algorithm on the
 159 Triton Shared Computing Cluster (TSCC) at the San Diego Supercomputer
 160 Center (San Diego Supercomputer Center, 2025). In Section 5, this statis-
 161 tically estimated model is used to compute the associated MPEMP. Section
 162 6 contains a list of challenges that need to be overcome before such models
 163 can be widely used to identify extinction-avoiding management plans. Some
 164 conclusions are reached in Section 7.

165 2. An Integrated Political-Ecological Model

166 2.1. Why do submodels need to be integrated?

167 Given a model composed of political submodels and an ecosystem sub-
 168 model, if actions that are generated by political submodels do not impact the
 169 ecosystem submodel at model-generated time points – and ecosystem sub-
 170 models actions do not in-turn, affect these political submodels, then feedback
 171 loops between political processes and ecological processes cannot emerge.

For instance, if a climate model is exogenously set to a schedule of reductions in carbon emissions forcing, there is no mechanism for modelling the vicissitudes of political support for climate policy. Such vicissitude might take the form of a sequence of governmental administrations alternately supporting and then not supporting climate change mitigation policies. The jagged time series of carbon emissions that results from this support-nonsupport policy record cannot be realistically simulated unless this sequence of different administrations and the effects of their actions on earth’s climate is represented in the simulation model. Hence, there needs to be an *integrated* model of political processes interacting with ecological processes. In this article, the main ecological process that needs to be modeled is the population dynamics of an at-risk species.

2.2. *Advantages of an individual-based model of an at-risk species*

As Netz et al. (2022) note,

“To allow for mathematical analysis, models of predator–prey co-evolution are often coarse-grained, focussing on population-level processes and largely neglecting individual-level behaviour. As selection is acting on individual-level properties, we here present a more mechanistic approach: an individual-based simulation model for the coevolution of predators and prey on a fine-grained resource landscape, where features relevant for ecology (like changes in local densities) and evolution (like differences in survival and reproduction) emerge naturally from interactions between individuals” (Netz et al., 2022).

2.3. *Example: The East African cheetah population*

The cheetah is listed as Vulnerable on the IUCN Red list and as Endangered by the Namibian government (Milloway, 2025). World Population (2025) reports 938 cheetah in Tanzania and 715 in Kenya. These two countries share a border and hence have the potential of interacting with each other politically. Therefore, as an example, a political-ecological model is built of the cheetah-hosting political-ecological system enclosed by these two countries. This model consists of submodels of several groups that affect

204 the cheetah population, and an ecosystem submodel of East African chee-
205 tah population dynamics. All of these submodels interact with each other
206 through time.

207 This agent/individual-based political-ecological model of the cheetah-
208 hosting ecosystem contained within Kenya and Tanzania, is new.

209 *2.3.1. Submodels interact through a bulletin board*

210 At each time step, each group submodel and the ecosystem submodel
211 read actions directed against themselves from a bulletin board. Conditional
212 on a read-in input action, a group submodel computes the expected value of
213 *overall goal attainment* that they believe they will receive if they implement a
214 particular action-target combination. After making this computation for all
215 action-target combinations in their repertoire, they post to the bulletin board
216 the combination that has the highest expected overall goal attainment. The
217 Ecosystem Management Actions Taxonomy (EMAT) (Haas, 2024b) dictates
218 what actions a submodel recognizes and what it holds in its repertoire of
219 output actions.

220 The ecosystem submodel reacts to actions directed against it by adjusting
221 its output of cheetah and prey abundance across time.

222 *2.3.2. Group submodels*

223 Submodels represent Kenya’s presidential office, the Kenya Wildlife Ser-
224 vice, the rural residents of Kenya, and the pastoralists of Kenya. Simi-
225 lar submodels are constructed for Tanzania. A ninth group submodel is
226 constructed of a conservation-focused nongovernmental organization (NGO)
227 that runs conservation projects in both of these countries. Haas (2011, Chap-
228 ter 2), Haas and Ferreira (2017), and Haas (2025) detail the cognitive theory
229 and causal flow that these submodels use to decide what action to implement
230 based on their beliefs and those actions that have been directed against them
231 (called *input actions*). These group decision making submodels make deci-
232 sions that they believe will further their own set of goals without regard to the
233 goals of other groups and, except for the wildlife protection agency groups,
234 without regard to what effects their actions might have on the ecosystem or
235 the abundance of any particular species.

236 2.3.3. Cheetah-hosting ecosystem submodel

237 The ecosystem submodel tracks the dynamics of the trans-Kenya-Tanzania
238 cheetah population (abundance through time). This submodel interacts with
239 the above rural resident and pastoralist group submodels. Cheetah are indi-
240 vidually modeled following the individual-based model (IBM) paradigm. For
241 simplicity, however, this IBM interacts with a stochastic differential equation
242 (SDE) submodel of cheetah prey such as Thomson’s gazelle (*Gazella thom-*
243 *soni*) (Fitzgibbon, 1990). Both the cheetah IBM and the herbivore SDE
244 represent population dynamics stochastically.

245 This synthetic predator-prey submodel is new and extends a model de-
246 scribed in Kimbrell and Holt (2005).

247 Parameterization of this submodel follows a set of data-based values re-
248 ported in Kelly et al. (1998):

249 “Data are presented on the demography and reproductive suc-
250 cess of cheetahs living on the Serengeti Plains, Tanzania over a
251 25-year period. Average age at independence was 17.1 months,
252 females gave birth to their first litter at approximately 2.4 years
253 old, interbirth interval was 20.1 months, and average litter size
254 at independence was 2.1 cubs. Females who survived to inde-
255 pendence lived on average 6.2 years while minimum male average
256 longevity was 2.8 years for those born in the study area and 5.3
257 years for immigrants” (Kelly et al., 1998).

258 Working from this information, Table 1 contains the parameter values used
259 in the cheetah IBM and the prey SDE.

Parameter	Value
Cheetah	
Life expectancy	6.2 (females); 2.8 (males)
Age at maturity	1.42
Sexual maturity	2.4 (females)
Interbirth interval	1.675
Herbivores	
Initial abundance (minor poaching)	2250
(moderate poaching)	4500
(severe poaching)	8750
Birth rate – death rate (minor poaching)	-0.003
(moderate poaching)	-0.014
(severe poaching)	-0.017
White noise multiplier (minor poaching)	0.001
(moderate poaching)	0.001
(severe poaching)	0.001

Table 1: Ecosystem submodel parameter hypothesis values. Cheetah IBM parameter values are derived from Kelly et al. (1998). The temporal unit is *years*. The submodel uses only the averaged cheetah life expectancy (4.5 years). Submodel output of herbivore abundance depicts a negative trend through time that is influenced by the amount of herbivore poaching.

260 A data file is created based on estimated cheetah abundance reported in
261 World Population (2025).

262 3. A New Optimization Algorithm

263 A new optimization algorithm is introduced herein that combines Simu-
264 lated Annealing (SA) (Corana et al., 1987) and Multiple Dimensions Ahead
265 Search (MDAS) (Haas, 2020). This new algorithm is called Constrained
266 Stochastic Synchronous Coupled Simulated Annealing – MDAS (SA-MDAS).

267 3.1. Background

268 Consider an optimization problem wherein an objective function in n
269 dimensions (hereafter, *variables*) is to be *minimized*. A *black-box optimization*
270 *algorithm* can handle all types of deterministic objective functions without

271 assuming anything about their smoothness or presence of discontinuities. To-
272 date, however, there has been little work on the development of algorithms
273 that can optimize a noisy (hereafter, *stochastic*) black-box objective function.

274 As reviewed in Haas (2024), one algorithm that is capable of finding
275 the *global* solution to a deterministic black-box objective function is Parallel
276 Asynchronous Coupled Simulated Annealing (PACSA) of Gonçalves-e-Silva
277 et al. (2018). This algorithm however, does not recognize constraints and
278 is not designed for stochastic objective functions. Haas (2024) proposes for
279 future work, the development of a general purpose black-box optimization
280 algorithm that would handle *bound constraints* and, by incorporating the
281 algorithm of Branke et al. (2008) into PACSA, stochastic objective func-
282 tions. This envisioned program would compute statistical estimates of the
283 parameters of a political-ecological model. As explained next, however, a
284 combination of theory and computational experience has led to the devel-
285 opment of an algorithm that is different than the one envisioned in Haas
286 (2024).

287 One final background note: In the eighteenth century, the person who
288 organized an opera production was referred to as an *impresario*. The in-
289 dividuals who performed the opera be they singers, dancers, instrumental-
290 ists or conductors, were (and are) referred to as *performers* (Holmes, 1994).
291 These terms are used here to refer to different roles given by an optimiza-
292 tion algorithm to different compute nodes who collectively, make up a cluster
293 computer (Werstein et al., 2006).

294 3.2. Rationale for a new algorithm

295 In SA-MDAS, an impresario posts tasks to a *JavaSpace* (Haas, 2020)
296 for performers to take and complete. Once completed, a performer posts
297 a task’s results back to the *JavaSpace*. The impresario then takes these
298 results from the *JavaSpace* and uses them to decide where next to search.
299 Here, a *JavaSpace* is implemented via the *GigaSpaces* XAP (Ciatto et al.,
300 2020). SA-MDAS is implemented in the JAVA language because JAVA is
301 (a) computationally efficient; (b) easily parallelized; and (c) easy to read and
302 hence, easy to maintain (Haas, 2020).

303 When the cooling schedule of Aarts and Korst (1989) is employed within
304 PACSA, computational experience has shown that the use of equation (1) in

305 Gonçalves-e-Silva et al. (2018) causes the maximum accepted function value
 306 term to become large as iterations increase. This happens because some of
 307 the performers begin to return poor (large) objective function values when
 308 their solution chains enter suboptimal subspaces. This increased value of
 309 the maximum-function term causes the acceptance probability to become
 310 small – causing progress towards an optimal solution to essentially stop. For
 311 this reason, the asynchronous inter-performer coupling scheme developed in
 312 Gonçalves-e-Silva et al. (2018) is not used in SA-MDAS.

313 Regarding stochastic objective functions, Bouttier and Gavra (2019) pro-
 314 vide a convergence proof for their approach to handling such functions within
 315 an SA optimization algorithm. For this reason, the Bouttier and Gavra
 316 (2019) approach to handling stochastic objective functions is employed in
 317 SA-MDAS rather than the approach taken by Branke et al. (2008).

318 3.3. Algorithm summary

319 SA-MDAS uses both SA and MDAS to solve an optimization problem
 320 that has a (possibly) stochastic black box objective function and continuous
 321 variables that are bound-constrained. Implicit constraints are also accom-
 322 modated. To ensure finite-time convergence, SA-MDAS employs the cooling
 323 schedule of Aarts and Korst (1989, chapter 4).

324 SA-MDAS employs many performers in order to both increase the chance
 325 that a global solution is found, and to reduce the time it takes to find it, called
 326 the *wall clock time* (Jiang and Singh, 2010). This is accomplished in-part
 327 through a new method developed herein called Multiple Periodic Exchange
 328 (MPE) – a scheme similar to the class of parallel SA algorithms dubbed
 329 *periodic exchange schemes* by Lee and Lee (1996).

330 A well-known characteristic of SA is its slow rate of convergence (Guilmeau
 331 et al., 2021). This drawback is addressed in SA-MDAS by switching the
 332 search algorithm from a parallel SA-like search algorithm to a parallel Hooke-
 333 Jeeves-like search algorithm namely, MDAS.

334 The result of this *two-phase* architecture (Ferreiro et al., 2019) is an algo-
 335 rithm that takes advantage of SA’s global search capability enhanced through
 336 cluster computing – but that avoids SA’s proclivity for slow convergence by
 337 switching to an efficient local search algorithm (MDAS) that also leverages

338 a cluster computing environment. The switch happens only after significant
 339 effort has been directed towards finding a subspace that has a high likelihood
 340 of containing the global minimum. Specifically, this switch is delayed until
 341 the SA step length along any variable becomes so small that the likelihood
 342 of a move into a radically different subspace also becomes small.

343 The Appendix contains details of how SA-MDAS handles continuous vari-
 344 ables, stochastic objective functions, and messaging between compute nodes.
 345 This Appendix also contains comparisons of SA-MDAS with other optimiza-
 346 tion algorithms.

347 3.4. Algorithm

348 1. Global search phase:

- 349 (a) Set values for n_s (see Appendix), and the chain length. Also,
 350 find initial values for each variable's step length, and the control
 351 parameter t ("temperature"). Initialize this latter parameter so
 352 that the percentage of moves accepted is between 70 and 90. Run
 353 this task on the impresario compute node alone.
- 354 (b) Within SA's inner loop, start each of m performer nodes at the
 355 same initial solution.
- 356 (c) Run these performers simultaneously but independently over one
 357 Markov chain.
- 358 (d) Always accept solutions that deliver a score value that is smaller
 359 than *current_value*. Accept other solutions with probability

$$\exp \{-(\textit{trial_value} - \textit{current_value})/t\}. \quad (1)$$

- 360 (e) Block until all performers have finished their respective chains.
- 361 (f) Update the sample size used to compute the average value of a
 362 stochastic objective function. Also update each variable's step
 363 length.
- 364 (g) Update t via the rule developed in Aarts and Korst (1989, Chap-
 365 ter 4).
- 366 (h) Return if a solution has been found such that the score function
 367 has been reduced to 90% of its initial value. Otherwise, continue
 368 to Step i .

- 369 (i) Execute MPE by reinitializing every performer with the solution
- 370 that gave the current smallest score value.
- 371 (j) Go to Step *c*.
- 372 2. Local search phase:
- 373 (a) After the SA subalgorithm has returned, use the returned solution
- 374 as the starting solution in an MDAS run. Set the MDAS algorithm
- 375 to search forward three variables at a time.
- 376 (b) Run MDAS to convergence and then stop.

377 3.5. SA-MDAS performance on analytic objective functions

378 Haas (2020) reports that MDAS correctly solves Bukin’s F4 function
 379 (Mishra, 2006). Using $n_s = 60$ (Corana et al., 1987), a chain length of
 380 10, and 10 performers, SA-MDAS finds the global minimum solution to
 381 Bukin’s F4 function in 12,353 objective function evaluations. SA-MDAS
 382 fails to find the global minimum solution for Bukin’s F6 function. But when
 383 the global search phase of SA-MDAS is allowed to run to convergence rather
 384 than switching to local search, the global minimum of this function is found
 385 after 4,716,030 function evaluations. Bukin’s F4 function has a pathological
 386 number of *non-global minima* (Hasanzadeh et al., 2022) – as does Bukin’s
 387 F6 function. Clearly, SA-MDAS is capable of finding the global minimum
 388 of a highly multi-modal function when nearly unlimited computing power is
 389 available.

390 Real-world functions are not necessarily as pathological as Bukin’s F6.
 391 Hence, the performance of SA-MDAS on Bukin’s F4 gives gives some credence
 392 to the idea that it can find nearly optimal solutions to real-world conservation
 393 optimization problems. To support this supposition, SA-MDAS is assessed in
 394 the next Section by seeing how well it statistically estimates the parameters
 395 of a political-ecological model built to represent a real world conservation
 396 challenge.

397 4. Statistical Estimation of a Political-Ecological Model

398 4.1. Overview of the CA estimator

399 The CA estimator of Haas (2011, Chapter 3) produces a set of *consis-*
 400 *tent* parameter values such that model output balances agreement with data

401 versus agreement with cognitive theories of decision making. To do this, an
 402 objective function is defined to be the priority-weighted sum of standardized
 403 measures of the agreement with a data set (g_S), and the agreement with
 404 the model’s joint probability distribution across its stochastic nodes (here-
 405 after, *distribution*) under *hypothesis* parameter values (g_H). The value of
 406 $ch \in (0, 1)$ is the relative priority given to having the *consistent* (estimated)
 407 model’s distribution agree with the one specified by the hypothesis parameter
 408 values – versus agreeing with the data (here, an observed actions history):
 409 $g_{CA} = (ch)g_H + (1 - ch)g_S$.

410 When ch is 0, CA becomes a frequentist statistical estimator. When ch
 411 is 1, CA finds parameter values that result in the model maximally agreeing
 412 with both decision making theory and with ecological theory that collectively,
 413 dictate how the political-ecological system ought to behave.

414 CA fits a model in two stages. Stage I consists of finding parameter values
 415 so that the model matches as many observed actions as possible. Then, this
 416 Stage I percentage of action-agreement (match fraction) is computed. Next,
 417 Stage II adjusts these Stage I parameter values until the model’s distribution
 418 is as close as possible to the hypothesis distribution while maintaining Stage
 419 I’s match fraction. The idea behind this two-stage approach is to minimize
 420 the occurrence of *jump discontinuities* (Schober and Prestin, 2023) caused by
 421 one or more group submodels switching to different action-target combina-
 422 tions due to a small change in a parameter’s value as the algorithm evaluates
 423 the objective function at different points in the solution space.

424 4.2. Objective function

425 Because of the above-mentioned potential for jump discontinuities, it is
 426 important to not accept any trial moves that reduce the match fraction from
 427 that achieved in Stage I. This agreement is enforced by adding a large penalty
 428 to the objective function if a move causes a reduction in the agreement with
 429 the observed actions history. Use of such a penalty function to, in-effect, rep-
 430 resent an implicit constraint, works in SA-MDAS because numerical insta-
 431 bilities that might be caused by explosive numerical derivative computations
 432 cannot happen because SA-MDAS does not compute such derivatives.

433 Stage II uses a stochastic agreement function for g_H that is the negative
 434 of the Hellinger distance between the consistent and hypothesis distributions.

435 Letting $P(P = i) = p_i$ (and $P(Q = i) = q_i$), for two discrete distributions,
 436 this distance is

$$H(P, Q) = \sqrt{\frac{1}{2} \sum_{i=1}^d (\sqrt{p_i} - \sqrt{q_i})^2} \quad (2)$$

437 where d is the number of discrete values that the random variable P (and Q)
 438 can take on (Suresh, 2021).

439 4.3. Stage I's action-matching algorithm

440 Stage I finds starting parameter values by executing two subalgorithms.
 441 The first subalgorithm entails the sequential matching of action-target com-
 442 binations with those observed. This subalgorithm is as follows.

- 443 1. At each time point, check the match between the observed action-target
 444 combination and the one generated by the group submodel. If they do
 445 not match, replace the submodel's action-target combination with that
 446 observed.
- 447 2. If this replacement causes the overall fraction of matches to become
 448 smaller, reject this replacement.
- 449 3. If the end-time has not been reached, go to the next group submodel
 450 or next time point. Otherwise, write this *desired actions history* to a
 451 file and exit.

452 The second subalgorithm proceeds by adjusting submodel parameters un-
 453 til model output matches as many action-target combinations in the desired
 454 actions history as possible – regardless of its agreement with the hypothesis
 455 distribution.

456 4.4. Results

457 SA-MDAS is used to statistically estimate parameter values of the political-
 458 ecological model of East African cheetah trafficking as follows.

459 4.4.1. Actions history

460 The STAR protocol of Haas (2024b) is used to collect actions reported in
 461 online press sources concerning cheetah management in Kenya and Tanzania.
 462 Doing so yields 105 actions over the time period 2019 through May 2025
 463 (Table 2).

Date	Actor	Action	Target(s)
2019.55	kenpas	starve_due_to_drought	kenpas
2019.71	kenrr	poach_for_food	three,kenpres,kenepa,ngo
2019.99	tanrr	poach_for_food	one,cheetaheco
2021.20	ngo	fund_rural_development_project	one,chetaheco
2022.17	kenepa	translocate_animals	one,chetaheco
2022.34	tanrr	plant_trees	one,cheetaheco
2023.67	kenrr	poach_for_cash	one,chetaheco
2023.73	kenrr	poach_for_food	three,kenpres,kenepa,ngo
2024.49	kenrr	poach_for_cash	one,chetaheco
2025.18	kenrr	poach_for_cash	one,chetaheco

Table 2: Selected political-ecological actions extracted from online sources with the STAR protocol of Haas (2024b)

4.4.2. Model fitting

The parameters that determine how likely Kenya rural residents and Tanzania rural residents think they will be arrested after they poach cheetah for cash are adjusted so that the model's output agrees with the observed actions history while exhibiting a joint probability distribution across its nodes that maximally agrees with the distribution defined to represent theoretical propositions about these beliefs. Adding-in parameters to represent Kenya pastoralist and Tanzania pastoralist beliefs is planned for future work.

Here, the hypothesis distribution values of these parameters represent the theory that a typical rural resident believes there is little chance they will have any interaction with police after they poach a cheetah for cash. Equal priority is given to agreement with the hypothesis distribution versus agreement with observations ($ch = 0.5$).

This CA is implemented as a 54-variable optimization problem. These variables are the parameters that determine the Scenario Imminent Interaction with Police (SIIWP) node in the Kenya rural resident submodel and the Tanzania rural resident submodel under the conditioning event that a rural resident decides to implement the output action, *poach cheetah for cash*.

SA-MDAS employed three performers with each performer accessing 10 threads when performing a parallel Monte Carlo simulation. Each such simulation required 1000 simulated realizations of a submodel's stochastic nodes. Such a simulation was run whenever a submodel received a new input action-target combination at some step in the time interval that the model was run over.

Because parameters in the ecosystem submodel were not being adjusted, in order to reduce wall clock time, ecosystem submodel calculations were turned off during this run of the SA-MDAS algorithm. Doing so reduced the objective function's evaluation time from 44 seconds to 15 seconds.

Due to a modest computing budget, the SA-MDAS algorithm was allowed to run for up to 3000 function evaluations during each phase. The run's wall clock time was 6.6 hours. Phase one converged after 2991 function evaluations, and phase two was terminated after completing 3043 function evaluations due to exceeding the maximum number of function evaluations. After the run had finished, the algorithm had increased the value of g_{CA} by

498 23.3% (Table 3).

499 At this solution, ecosystem computations were turned on and the ob-
500 jective function computed one final time (Table 4). Including the ecosystem
501 submodel defined by its hypothesis distribution parameter values significantly
502 affects the model's overall fit as quantified by g_{CA} (Table 4).

Agreement measure	Symbol	Initial value	Consistent value	Percent increase
Agreement with observed actions history (match fraction)	$g_S^{(Grp)}$	0.491	0.528	0.075
Agreement with observed cheetah abundance	$g_S^{(Eco)}$	-0.141	0.0	1.000
Average agreement between consistent group submodels and hypothesis submodels	$g_H^{(Grp)}$	-0.486	-0.419	0.138
Overall agreement	g_{CA}	-0.382	-0.294	0.230

Table 3: CA agreement measures before and after the SA-MDAS run wherein ecosystem computations were kept off during the computation of the final values. Agreement between the ecological submodel's consistent distribution and its hypothesis distribution is not computed because no parameters within this submodel are being estimated.

Agreement measure	Symbol	Initial value	Consistent value	Percent increase
Agreement with observed actions history (match fraction)	$g_S^{(Grp)}$	0.528	0.509	-0.360
Agreement with observed cheetah abundance	$g_S^{(Eco)}$	-0.141	-0.137	0.028
Average agreement between consistent group submodels and hypothesis submodels	$g_H^{(Grp)}$	-0.486	-0.419	0.138
Overall agreement	g_{CA}	-0.382	-0.338	0.114

Table 4: CA agreement measures before and after the SA-MDAS run with ecosystem computations turned on when computing the final values.

503 Figure 1 displays the actions history generated by the CA-estimated
504 model along with those observed actions that are matched by the CA-estimated
505 model. To exhibit typical interaction patterns that are obscured in Figure 1,
506 Figure 2 exhibits a closeup of the period from 2024 to 2025.

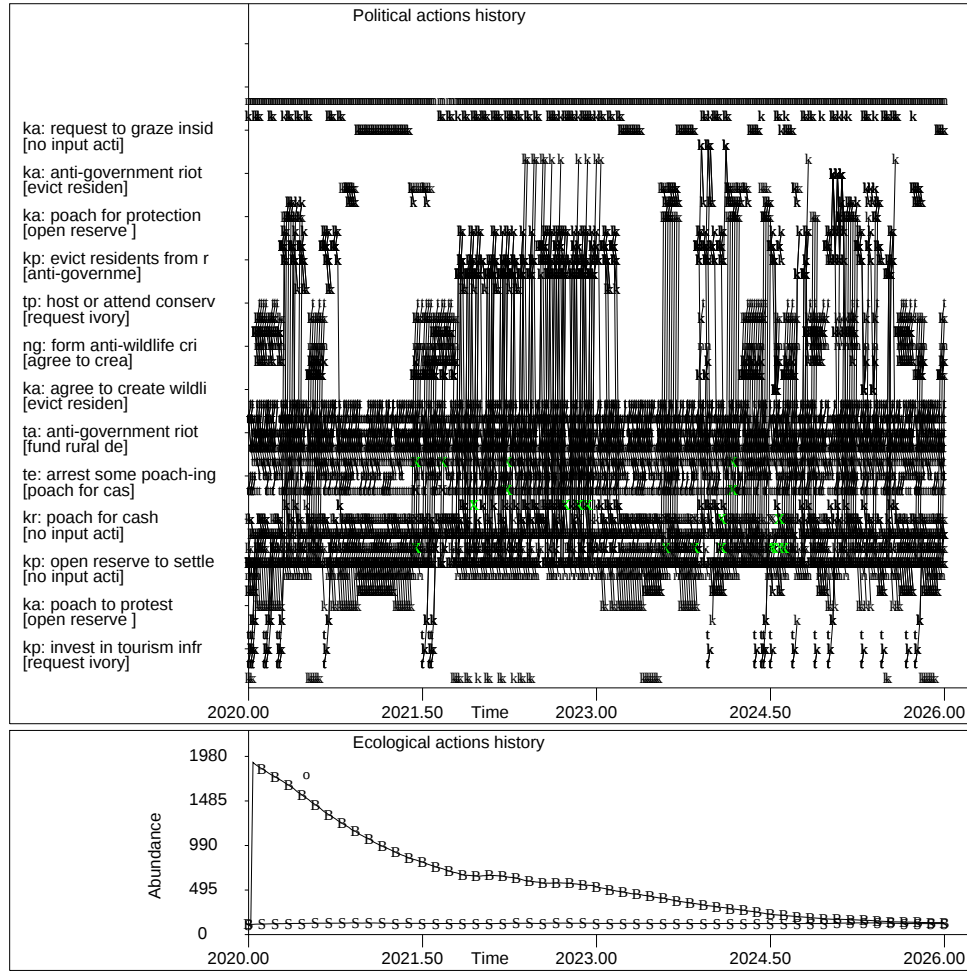


Figure 1: Model-generated actions history from 2020 through 2029. Green crosses are observed actions matched by the the CA-estimated model. The $\circ$ symbol denotes an observation on cheetah abundance.

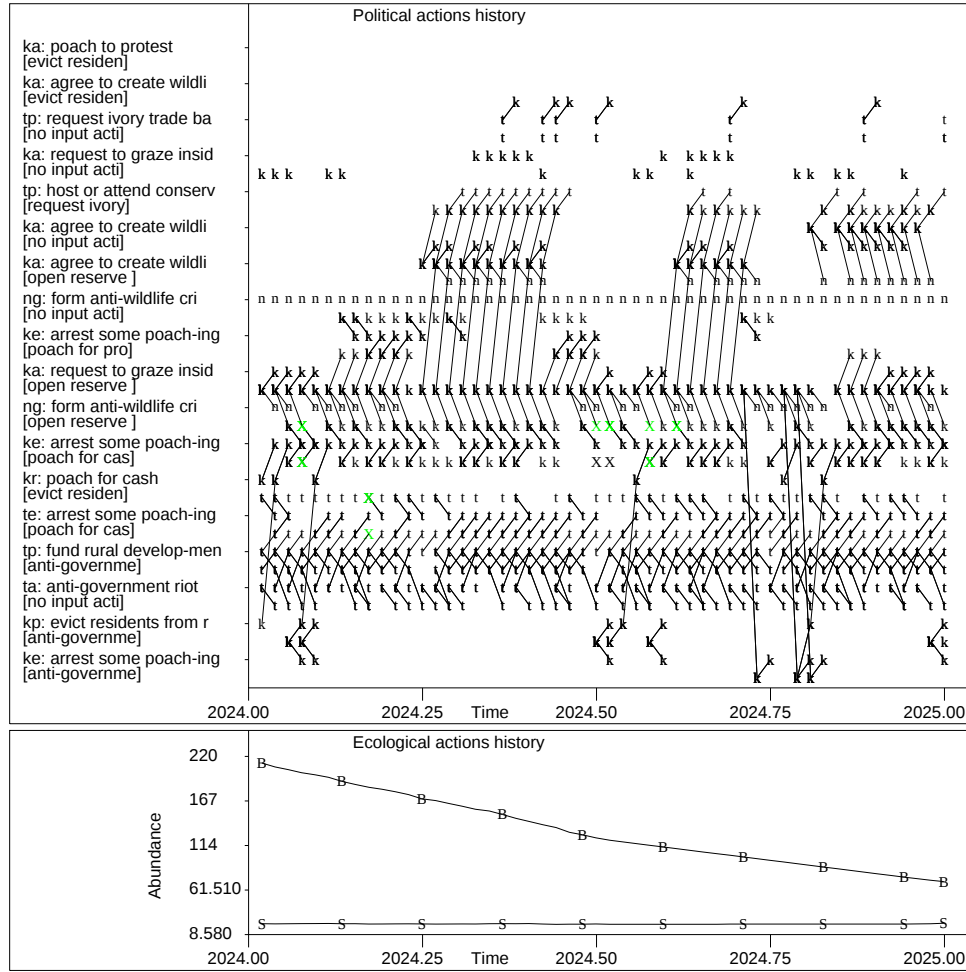


Figure 2: Model-generated actions history from 2024 to 2025.

507 This example shows that SA-MDAS can find CA estimates of a political-
508 ecological model's parameters in a practical amount of wall clock time.

509 5. Finding the MPEMP

510 Haas and Ferreira (2017) state that

511 “A more general method of developing management policies is the
512 *most practical ecosystem management plan* (MPEMP) of Haas
513 (2011, Chapter 4). The MPEMP emerges from the pattern of
514 group behaviors that results from modifying one or more group
515 belief systems. These modifications are such that the agreement

516 between group belief systems that are estimated from data – and
517 the belief systems that produce group actions that cause a desired
518 ecosystem state, is maximized. In other words, the MPEMP is the
519 sequence of group behaviors that occur from the least change in
520 existing group beliefs systems that still achieves ecosystem state
521 goals” (Haas and Ferreira, 2017).

522 Clearly, finding the MPEMP involves solving an optimization problem.
523 This optimization problem is constrained by the requirement that any solu-
524 tion needs to produce values of the ecosystem’s output variables that are close
525 to the desired values at the desired point in time. This implicit constraint
526 is incorporated into SA-MDAS as a penalty function in a manner similar to
527 the CA constraint of maintaining a maximal fraction of model-to-observed
528 action matches.

529 Only group submodel parameters can be variables in this constrained
530 optimization problem. CA-estimated parameter values are used as starting
531 values for all group submodels. During the optimization’s search, however,
532 all ecosystem submodel parameters are held at their CA-estimated values.
533 Doing so represents the assumption made in the MPEMP computation that
534 ecosystem dynamics are not under anthropogenic control but group belief
535 systems are. Therefore, realistic ecosystem management plans should be re-
536 stricted to making small modifications to human beliefs – and hence behavior
537 rather than attempting to make changes to those ecological mechanisms that
538 produce the modeled ecosystem’s dynamics.

539 The preferred solution to the MPEMP optimization problem is a local
540 one rather than a global one. This is because the MPEMP is the plan that
541 requires the least change in existing beliefs (as represented by the model’s
542 consistent distribution) needed to redirect human behaviors enough to allow
543 the ecosystem to reach a desired state. Hence, a solution that is close to the
544 existing set of beliefs needs to be found.

545 The objective function in an MPEMP optimization problem needs to in-
546 clude the ecosystem submodel. This because the effect of group actions on
547 the ecosystem needs to be detected every time the objective function is eval-
548 uated. Including the ecosystem submodel in the political-ecological model’s
549 simulation, however, can increase the objective function’s evaluation time.

Further, when the ecosystem submodel is stochastic as in the East African cheetah example herein, the method of Bouttier and Gavra (2019) for solving a stochastic, black-box optimization problem needs to be employed. This method involves taking the average of repeated evaluations of the stochastic objective function at a trial solution point. This averaged value has a smaller variance than the original stochastic objective function.

The above discussion reveals that there are two computationally expensive factors that complicate the evaluation of an MPEMP objective function. These are: The need to include the ecosystem submodel in the political-ecological model's simulation, and the need to compute an average over several function calls each time the optimization algorithm requires an objective function value. These two factors can cause the MPEMP objective function to have a long evaluation time. For instance, in the example below, the objective function's evaluation time is about 59 seconds. This long evaluation time in-turn, causes a long wall clock time before a solution to the MPEMP optimization problem is found. And long wall clock times can be expensive.

5.1. MPEMP algorithm

5.1.1. Needed definitions

1. The vector

$$\mathcal{B} = \left[\mathcal{B}^{(Grp)'} \mathcal{B}^{(Eco)'} \right]'$$

contains parameters of the group submodels, and the ecosystem submodel, respectively.

2. Let the vector, $\mathbf{Q}(\mathcal{B})$ contain the monitored ecosystem submodel variables whose values are generated by the ecosystem submodel using parameter values contained in $\mathcal{B}$.
3. Let $\mathbf{q}_d$ contain the desired ecosystem state in terms of $\mathbf{Q}(\cdot)$ along with the time when these values are to be achieved.
4. Identify those actions that, if taken, would contribute the most towards the ecosystem submodel producing the values in $\mathbf{q}_d$. And, identify those actions that, if ceased, would raise the likelihood of the ecosystem submodel producing the values in $\mathbf{q}_d$. Collect all of these desirable and undesirable actions into a set called $\mathbf{c}_{MPEMP}$.

581 *5.1.2. Algorithm*

582 The following mathematical form of the MPEMP algorithm extends the
583 one reported in Haas (2020).

- 584 1. Compute CA estimates of selected model parameters, i.e., up-
585 date $\mathcal{B}_H$ to the most recent set of consistent parameter values:
586 $\mathcal{B}_C$.
- 587 2. Compute $\mathbf{q}_H \equiv E[\mathbf{Q}(\mathcal{B}_H)]$.
- 588 3. Specify $\mathbf{q}_d$ and $\mathbf{c}_{MPEMP}$.
- 589 4. Compute initial values for $\mathcal{B}^{(Grp)}$ with CA's **Initialize** step.
- 590 5. Compute

$$\mathcal{B}_{MPEMP} = \arg \max_{\mathcal{B}^{(Grp)}} \left\{ g_H^{(Grp)}(\mathcal{B}) - \frac{\|E[\mathbf{Q}(\mathcal{B})] - \mathbf{q}_d\|}{\|\mathbf{q}_H - \mathbf{q}_d\|} \right\} \quad (3)$$

591 under the set of constraints specified by $\mathbf{c}_{MPEMP}$.

592 Note that during the search in Step 5, $\mathcal{B}_H^{(Eco)}$ is unchanged.

593 *5.1.3. Quantifying political feasibility*

594 The MPEMP algorithm implements one way to quantify the concept of a
595 politically feasible ecosystem management plan: Associate political feasibility
596 with $g_H(\mathcal{B}_{MPEMP}^{(Grp)}) \in (-\infty, 0]$ where $\mathcal{B}_{MPEMP}^{(Grp)}$ contains the parameters of
597 the decision making submodels whose values have been modified from those
598 in $\mathcal{B}_H^{(Grp)}$ in such a way that now, the sequence of output actions taken by the
599 different groups in the model causes a desired ecosystem state at a desired
600 future time point ($\mathbf{q}_d$).

601 A measure of a plan's political feasibility can be defined as

$$\psi \equiv g_H^{(Grp)}(\mathcal{B}_{MPEMP}^{(Grp)}) / (|g_H^{(Grp)}(\mathcal{B}_H)| + 0.000001). \quad (4)$$

602 The numerator is the agreement of the MPEMP distribution with the hy-
603 pothesis distribution where large negative values indicate poor agreement.
604 The first term in the denominator is the absolute value of the agreement of
605 the model's distribution with the hypothesis distribution – using parameter
606 values from the hypothesis distribution itself. When approximation error is
607 zero, this term is zero. Hence, $g_H^{(Grp)}(\mathcal{B}_{MPEMP}^{(Grp)}) \leq |g_H^{(Grp)}(\mathcal{B}_H)|$.

608 A plan having a value of $\psi \ll -1.0$ will face stiff political resistance to
 609 its implementation because significant changes to the belief systems of one
 610 or more groups needs to happen – while a plan having a value close to -1.0
 611 should not face such strong political headwinds.

612 5.2. Results

613 The desired ecosystem state is 800 cheetah across Kenya and Tanzania
 614 in the year 2029.

615 The parameters to be modified during the search for the MPEMP are
 616 those used in the above CA example with the addition of the parameters
 617 defining the node: Number of Cheetah Poached (NMPOACHED) under the
 618 proposed action of *poach cheetah for protection* for both Kenya rural residents
 619 and Tanzania rural residents.

620 These parameters are included in the MPEMP computation in order to
 621 study the feasibility of a two-pronged approach to cheetah conservation: Dis-
 622 couraging rural residents from poaching cheetah for cash while at the same
 623 time increasing antipoaching measures. To these ends, the SIIWP paramete-
 624 rs are included to guide the amount of belief-change that would be needed
 625 to discourage rural residents from poaching cheetah for cash – and the NM-
 626 POACHED parameters to find the needed increase in antipoaching measures
 627 to stop rural residents from poaching cheetahs for protection. Optimizing
 628 these two sets of parameters simultaneously results in smaller changes to
 629 these parameters relative to the changes that would be required if only one
 630 of these sets was changed without changing the other. And smaller changes
 631 give the plan greater political feasibility.

632 In summary, the CA estimation modifies the SIIWP parameters concern-
 633 ing *poach cheetah for cash*. The MPEMP computation modifies the SIIWP
 634 parameters concerning *poach cheetah for cash* and the NMPOACHED pa-
 635 rameters conditional on *poach cheetah for protection*.

636 5.2.1. MPEMP computation

637 To begin the optimization computation at a feasible solution, initial values
 638 of the SIIWP parameters were modified to produce the following output
 639 actions by both the Kenya rural resident group, and the Tanzania rural
 640 resident group: no *poach cheetah for cash* actions, no *poach cheetah for food*

actions; but high probabilities for the actions, *poach cheetah for protection*, and *protest national park boundaries*.

Due to a modest computing budget, the sample size for averaging values of the stochastic objective function was fixed at three for the entire run. Not allowing this sample size to increase each pass through SA’s outer loop means that the convergence proof of Bouttier and Gavra (2019) is only partially satisfied for this run. This proof states that if the algorithm of Bouttier and Gavra (2019) is followed, SA will converge to the global minimum of the stochastic objective function’s expected value. Had this sample size been allowed to increase every pass through SA’s outer loop, it would have equalled 39 when phase one finished.

Running on the TSCC, the SA-MDAS algorithm was restricted to 3000 objective function evaluations for each phase. The run employed three performers executing on 10 threads each. The run’s wall clock time was 8.8 hours. The initial MPEMP objective function value was -0.779, and the final value was -0.711 for a 8.66% increase. Phase one converged after 1661 function evaluations and phase two terminated after 3037 function evaluations because it had exceeded its maximum number of function evaluations.

5.2.2. The computed MPEMP

This run produced an MPEMP that is projected to allow an expected cheetah population size of 278 by 2029. This is short of the desired goal of 800 cheetah by 2029 but avoids the forecast extinction event at the end of 2029 under the business-as-usual plan. The measure of the plan’s political feasibility, ψ was computed to be -1.025.

Tables 5 and 6 show each parameter’s definition, its CA value, and its MPEMP value. These parameter value changes indicate that the MPEMP is to (a) change the belief in being arrested for poaching cheetah for cash from being perceived as negligible to being perceived as likely; and (b) increase antipoaching measures to the point where Kenya and Tanzania rural residents each succeed in poaching less than six cheetah per week.

The number of cheetah poached per week by Kenya rural residents and the number of cheetah poached per week by Tanzania rural residents were not adjusted by the CA. Hence, these two parameters were held at their hypothesis values. These hypothesis values are slightly below the upper

675 bound constraint shared by these parameters. This upper bound value is
676 six. This value indicates a significant amount of poaching that aligns with
677 the hypothesis-belief held by these rural residents that they will not be ar-
678 rested for poaching cheetah.

Parameter	Node	CA value	MPEMP value	Change fraction	> 10% change?
1	Number_Poached	5.994	3.574	00.403	*
2	SIIWP	00.274	00.193	00.294	*
3	SIIWP	00.356	00.232	00.347	*
4	SIIWP	00.369	00.573	00.555	*
5	SIIWP	00.054	00.320	4.926	*
6	SIIWP	00.346	00.357	00.029	
7	SIIWP	00.599	00.322	00.461	*
8	SIIWP	00.166	00.553	2.337	*
9	SIIWP	00.402	00.119	00.702	*
10	SIIWP	00.431	00.326	00.244	*
11	SIIWP	00.410	00.036	00.911	*
12	SIIWP	00.133	00.739	4.558	*
13	SIIWP	00.455	00.224	00.507	*
14	SIIWP	00.346	00.329	00.047	
15	SIIWP	00.056	00.329	4.878	*
16	SIIWP	00.598	00.341	00.429	*
17	SIIWP	00.175	00.461	1.634	*
18	SIIWP	00.292	00.373	00.280	*
19	SIIWP	00.533	00.165	00.690	*
20	SIIWP	00.242	00.535	1.214	*
21	SIIWP	00.490	00.337	00.310	*
22	SIIWP	00.268	00.126	00.528	*
23	SIIWP	00.118	00.403	2.387	*
24	SIIWP	00.253	00.202	00.199	*
25	SIIWP	00.628	00.394	00.372	*
26	SIIWP	00.306	00.197	00.355	*
27	SIIWP	00.400	00.660	00.647	*
28	SIIWP	00.292	00.142	00.515	*

Table 5: Kenya rural resident parameter value changes needed to produce the MPEMP. The first parameter is the average number of cheetah poached per week by Kenya rural residents. The second set of parameters define the perceived outcome by Kenya rural residents under the decision option to *poach cheetah for cash*. Perceived outcomes are *will be arrested for poaching*, *will be evicted*, and *no interaction with police*.

Parameter	Node	CA value	MPEMP value	Change fraction	> 10% change?
29	Number_Poached	5.994	5.372	00.103	*
30	SIIWP	00.039	00.328	7.423	*
31	SIIWP	00.521	00.183	00.647	*
32	SIIWP	00.439	00.487	00.108	*
33	SIIWP	00.330	00.552	00.675	*
34	SIIWP	00.296	00.406	00.368	*
35	SIIWP	00.373	00.040	00.890	*
36	SIIWP	00.250	00.370	00.474	*
37	SIIWP	00.024	00.403	15.802	*
38	SIIWP	00.725	00.226	00.687	*
39	SIIWP	00.289	00.318	00.103	*
40	SIIWP	00.099	00.310	2.137	*
41	SIIWP	00.612	00.370	00.394	*
42	SIIWP	00.272	00.290	00.068	
43	SIIWP	00.400	00.352	00.118	*
44	SIIWP	00.328	00.356	00.087	
45	SIIWP	00.450	00.082	00.817	*
46	SIIWP	00.167	00.446	1.674	*
47	SIIWP	00.382	00.471	00.233	*
48	SIIWP	00.209	00.540	1.586	*
49	SIIWP	00.471	00.240	00.491	*
50	SIIWP	00.319	00.219	00.313	*
51	SIIWP	00.153	00.335	1.190	*
52	SIIWP	00.290	00.290	00.000	
53	SIIWP	00.557	00.374	00.327	*
54	SIIWP	00.132	00.320	1.426	*
55	SIIWP	00.048	00.252	4.259	*
56	SIIWP	00.820	00.427	00.478	*

Table 6: Tanzania rural resident parameter value changes needed to produce the MPEMP. The first parameter is the average number of cheetah poached per week by Tanzania rural residents. The second set of parameters define the perceived outcome by Tanzania rural residents under the decision option to *poach cheetah for cash*. Perceived outcomes are *will be arrested for poaching*, *will be evicted*, and *no interaction with police*.

679 5.2.3. *The MPEMP's political consequences*

680 Because of ψ 's modestly negative value, this MPEMP is expected to
681 face moderate political resistance. A practical policy for implementing this
682 MPEMP is to simultaneously (a) visibly increase antipoaching enforcement
683 in both countries, and (b) communicate such increases to the rural residents
684 of Kenya and Tanzania (Kegamba et al., 2024), (Nachihangu et al., 2022).

685 This fitted model and the political insights derived from it, are new.

686 5.3. *The MPEMP compared to other conservation planning tools*

687 5.3.1. *Marxan*

688 Marxan helps users select a set of conservation reserves (hereafter, a set
689 of *reserve patches*) that satisfy ecological, social, and financial goals. The
690 Marine Spatial Planning group at the Nature Conservancy gives this overview
691 of Marxan:

692 “Marxan is decision support software for designing new reserve
693 systems, reporting on performance of existing reserve systems,
694 and developing multiple-use zoning plans. It is the most widely
695 adopted site selection tool by conservation groups globally. Marxan
696 is a stand-alone software program that provides decision support
697 to teams of conservation planners and local experts identifying
698 efficient areas that combine to satisfy a number of ecological, so-
699 cial and economic objectives. Given data on species, habitats,
700 ecosystems and other biodiversity features, Marxan was designed
701 to minimize the cost of selected sites while meeting all goals (Ma-
702 rine Spatial Planning (2025)).”

703 Marxan finds these plans by solving the *set covering problem* (Liang et al.,
704 2020), (Watts et al., 2021). Marxan is strictly spatial in that the tool does not
705 recognize any temporal component in the spatial data it is given. Also, the
706 user provides all parameter values and Marxan makes no effort to incorporate
707 parameter uncertainties into its final solution. The only conservation plans
708 that Marxan can deliver are maps identifying the location and geometry of
709 each reserve patch.

710 Once computed, these reserve patches will presumably be forced onto
711 landscape residents by authoritarian actions such as the purchase of land or

712 the successful lobbying for the conversion of privately-held real estate into
713 reserve patches.

714 The MPEMP by comparison, emerges from the political realities sur-
715 rounding a biodiversity conservation challenge and allows plans to include
716 non-command-and-control solutions such as community-led changes in lan-
717 duse on private, non-reserve lands.

718 Marxan assumes that different sets of reserve patches can be mandated
719 without requiring community acceptance of the plan. In other words, Marxan
720 does not have readily-available inputs to represent data-derived political
721 forces that determine the political feasibility of mandating a set of reserve
722 patches. On the other hand, the central capability of the MPEMP construc-
723 tor is its ability to model these forces and their effects on the management
724 of an ecosystem.

725 The set covering problem is a classic, simple, linear, binary integer pro-
726 gramming problem (Liang et al., 2020). Continuously-valued metrics are not
727 allowed, nonlinear objective functions are not allowed, and integer variables
728 with more than two values are not allowed. Marxan runs on a single-CPU
729 computer. Hence, its ability to solve its set covering problem is, by design,
730 computationally limited. Unfortunately, the set covering problem is known
731 to be NP-hard (Liang et al., 2020) meaning that finding a solution to a com-
732 plex planning problem involving many possible sets of reserve patches can
733 take many months of wall clock time on a single-CPU computer to reach the
734 optimal solution.

735 But real-world reserve-set planning problems usually involve many pos-
736 sible solutions. This is similar to the set of possible plans for effectively
737 protecting an ecosystem within a larger political-ecological system – the prob-
738 lem that the present article solves. In contrast to Marxan, the present article
739 has tackled this crippling computational-expense roadblock head-on with its
740 cluster computing-based algorithm, SA-MDAS. SA-MDAS is designed to find
741 the MPEMP in a practical amount of wall clock time as opposed to the sev-
742 eral months of wall clock time that Marxan might spend in order to find an
743 optimal set of reserve patches.

744 5.3.2. Zonation 5

745 The Finnish Environment Institute describes Zonation as follows:

746 “The Zonation software enables prioritisation analyses of conser-
747 vation values based on spatial data to support decision-making,
748 conservation area planning, and the avoidance of negative eco-
749 logical impacts. It can incorporate a wide range of data, includ-
750 ing information on uncertainties and connectivity. The analyses
751 can be highly detailed and extensive, depending on the available
752 datasets (Finnish Environment Institute, 2025).”

753 In addition, Moilanen et al. (2022) describe the newest version of this spatial
754 conservation planning tool: *Zonation Version 5*.

755 Similar to Marxan, this tool helps the user to identify a set of reserve
756 patches within a given landscape. Differing from Marxan, however, this
757 tool does not explicitly solve an optimization problem in order to find a
758 set of patches that optimally meet a collection of target values on selected
759 ecological metrics. Rather, Zonation 5 performs a nested, two-level sort on
760 a large number of spatial units that collectively make up a landscape. This
761 sorting operation produces a ranked list of reserve patch geometries. Many
762 assumptions are made about what is ecologically preferred in order to place
763 enough characteristics on each spatial unit to allow the sorting algorithm to
764 compute rank-differences between spatial units. As with Marxan, Zonation 5
765 is strictly spatial in that the tool does not recognize any temporal component
766 in the spatial data it is given.

767 Because Zonation 5 employs an efficient sorting algorithm, it can quickly
768 rank-order a large number of spatial units on a single-CPU computer. Zona-
769 tion 5 does allow some political forces to impact its solutions by allowing the
770 user to input a set of “local preferences.” As with Marxan, however, the user
771 provides all parameter values with Zonation 5 making no effort to incorpo-
772 rate parameter uncertainties into its final rank-ordering of possible reserve
773 patch geometries.

774 As an aside, in actuality, sorting can be cast as an optimization problem
775 solved with a greedy search algorithm (Bauckhage and Welke, 2022). It is
776 the greedy nature of the search algorithm that allows Zonation to perform
777 efficient sorts on a single-CPU computer.

778 5.3.3. *Assessment*

779 These two tools only deliver a set of reserve patches across a given land-
780 scape. Neither tool allows, as the MPEMP computation does, a user to
781 model the political-ecological system that the landscape is a part of – let
782 alone provide a capability for statistically fitting such a model’s parameters
783 to a political-ecological data set.

784 A major drawback that makes these tools insufficient in light of current
785 political realities is their inability to allow a user to explore alternate con-
786 servation plans that might involve initiatives that are not a command-and-
787 control gazetting of land into reserve patches. Initiatives such as developing
788 alternate livelihoods, installing wildlife control fencing, increasing antipoach-
789 ing efforts, relocating animals, shooting marauding elephants, eradicating
790 invasive plants, donating antipoaching equipment, planting trees, restor-
791 ing mine tailings areas, compensating farmers for wildlife damages, and the
792 downgrading, downsizing, and degazettement of protected areas (PADDD)
793 Albrecht et al. (2021) – are not part of either tool’s plan repertoire. See the
794 file `emat.dfn` in the Supplementary Materials file, `MPEMP_constructor.zip`
795 for a complete list of such alternate conservation actions as gleaned from
796 political-ecological data acquired using the STAR protocol of Haas (2024b).

797 The critical deficiency of both of these tools, however, is that because all
798 priority weights are user-specified, any plan delivered by either tool, unlike
799 the MPEMP, lacks a data-derived, real-world measure of the plan’s political
800 feasibility.

801 6. Challenges

802 Before political-ecological modelling of global extinction events can guide
803 conservation efforts, several challenges need to be overcome. Below is a
804 priority-ordered list of some of these challenges.

- 805 1. Collaboration with the private sector is needed in order to tap their dis-
806 tributed autonomy; enormous reserves of talent; and enormous reserves
807 of cash and credit (Haas, 2022), (Haas, 2024c), (Haas, 2025).
- 808 2. Better political-ecological data sets need to be acquired that, via clus-
809 ter computer computations, can be used to statistically fit the param-

eters of these extinction event models. On the political side, observations need to be acquired on those private political agreements that often determine the fate of conservation legislation. On the ecological side, unrestricted and noninvasive monitoring of species abundance is needed. Currently, such data is often restricted because (a) owners refuse access to their properties, and/or (b) data managers fear that poachers will hack into the data's repository in order to locate wildlife (Lennox et al., 2020).

3. In order to make the statistical fitting of these models feasible to a wide spectrum of researchers, cluster computing resources need to be financially accessible to cash-strapped departments of ecology and departments of political science.

One economical alternative to purchasing time on a commercial cluster computer is to organize some number of in-house computers into a cluster computer. With the JavaSpaces-based SA-MDAS algorithm, this is a straightforward four-step build:

- (a) Install on an impresario, a *dynamic domain name system* (DDNS) (mintdns, 2023) in order to give this computer a fixed domain name so that performers can locate its GigaSpace. A DDNS is acquired from an internet provider or from a DDNS provider. Fees can be either none; a fixed monthly charge; or a monthly, usage-based charge.
- (b) Verify that all performers can access the internet.
- (c) Install the JAVA Development Kit (free) and the GigaSpaces XAP (annual lease) on the impresario and all performers.
- (d) Compile and run on these computers, the JAVA code exercised in this article.

4. The credibility of political-ecological models in the eyes of their skeptics needs to be established by meeting Popperian credibility criteria that are based on frequentist statistical methods (Haas, 2024) – rather than relying on the lobbying efforts of *activist scientists* (Whipple, 2024). Such rigorous, statistically-based model validation results are needed to maximize the acceptance by the general public of extinction-event predictions. This would be in contrast to the acceptance of the declarations made by the authors of climate models concerning the causes

845 of climate change. For instance, fewer than 50% of Americans believe
 846 that climate change is driven by anthropogenic forces (EPIC, 2023) –
 847 the central mechanism that is programmed into almost all mainstream
 848 climate models. In order to marshal the necessary support for expen-
 849 sive biodiversity conservation projects, a much higher proportion of
 850 popular support will be needed than what is given to climate change
 851 mitigation policies.
 852 Indeed, climate models do not currently meet rigorous statistical mea-
 853 sures of model credibility. For instance, Michaels (2019) notes that
 854 recent research indicates that the averaging of predictions across many
 855 different climate models as is routinely reported by the Intergovern-
 856 mental Panel on Climate Change (IPCC), increases prediction errors.
 857 This author suggests that work should focus on developing a single
 858 model that has low prediction errors. And Jain et al. (2023) find sig-
 859 nificant errors in model predictions of observed weather and suggest
 860 more computing resources may be needed to reduce this error.
 861 A literature search failed to find a peer-reviewed article that reports
 862 on a climate model that produces predictions of out-of-sample obser-
 863 vations to any specific, quantified level of accuracy. Nonetheless, such
 864 models are routinely used to justify climate-change mitigation policy
 865 decisions. This use of incompletely validated climate models has only
 866 fueled skepticism about the credibility of climate models. These skept-
 867 ics instead, suspect that climate change policymaking is being driven
 868 by flawed models (Montford, 2022). Indeed, in a particularly worrisome
 869 passage, Montford mentions the current practice of “tuning” model pa-
 870 rameters to increase a climate model’s agreement with observations.
 871 Such tuning is outside any frequentist-based statistical method of pa-
 872 rameter estimation.
 873 5. Group decision making mechanisms need to be better understood. Such
 874 newly-derived mechanisms need to be programmed into each group de-
 875 cision making submodel that runs within a political-ecological model.
 876 Also, computational models need to be developed that, through im-
 877 proved architectures, realistically integrate political and ecological pro-
 878 cesses. One such architecture employed herein is that of agent-based

879 submodels communicating with each other and with an individual-
880 based ecosystem submodel through a bulletin board.

881 6. Increased financial and career support is needed for interdisciplinary
882 research on the integration of political and ecological processes. Within
883 academia, this support will be aided when (a) journal editors encourage
884 the publication of high-quality manuscripts that probe this interface
885 (Huber-Sannwald, 2025), (O'Connor et al., 2021), (Van Bael, 2025);
886 and (b) departmental committees encourage tenure-track faculty to
887 publish at this interface (Washbourne et al., 2024). Outside academia,
888 funding agencies need to seek out and fund high-quality proposals to
889 build and test models of those political-ecological systems that contain
890 at-risk species.

891 7. Conclusions

892 For purposes of biodiversity conservation, attention needs to focus on
893 finding politically feasible projects aimed at conserving biodiversity. Earth
894 is running out of time to save what remains of its biodiversity. MPMPs
895 need to be computed and implemented as soon as possible. This article
896 shows that, thanks to the new optimization algorithm introduced herein,
897 these computations are now feasible. Indeed, as explained in the Appendix,
898 an optimization algorithm such as SA-MDAS that scales on the increasing
899 availability of cluster computer nodes, is currently, the only feasible way to
900 statistically fit a large political-ecological model to data.

901 The political-ecological models that will support these projects, can have
902 their parameters statistically estimated via CA to political-ecological data
903 sets acquired via the STAR protocol of Haas (2024b). Use of CA to perform
904 this parameter estimation, allows cognitive theories of decision making to be
905 represented in the final fitted models.

906 As per this article's title, the MPMP is how a political-ecological model
907 can help sustain biodiversity. The freely available MPMP constructor can
908 be immediately used by an organization to develop and implement politically
909 feasible and ecologically effective plans for conserving those at-risk species
910 that they have selected to help preserve.

911 Given the current negative trends in biodiversity, one might conclude
912 that conservation research is futile and hence, should be abandoned. A re-
913 cent meta-analysis, however, using data from many different conservation
914 projects, finds that actually, conservation projects have been effective at
915 stopping or at least slowing the decline of biodiversity across the globe (Ox-
916 ford, 2024). Given this evidence, there is reason to believe that research
917 products such as the MPEMP constructor offered in this article, can help
918 build a conservation science that is capable of guiding successful efforts to
919 curb the loss of species regardless of their commercial value.

920 **Supplementary material**

921 All source code and input files that constitute the MPEMP constructor
922 described and exercised in this article are contained in the Supplementary
923 Material files `idsrce.zip` (JAVA source code), and `MPEMP_constructor.zip`
924 (linux shell scripts, input command files, and data files).

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1206 Appendix: SA-MDAS Details and Comparisons

1207 *Continuous variables*

1208 All parameters in the political-ecological model studied in Section 4 are
1209 continuous. Hence, a method is needed for applying SA to continuously-
1210 valued variables. Here, the method developed in Corana et al. (1987) is used.
1211 One way to specify the length of SA’s Markov chain, i.e., the number of passes
1212 through SA’s inner loop, is to define it to be the size of the neighborhood
1213 surrounding the current solution point (Aarts and Korst, 1989, p. 65), i.e.,
1214 the number of points reachable in one move. Given a small step length, the
1215 number of possible solution space points accessible in one move can become
1216 large.

1217 Corana et al. (1987) take a different approach. They define their n_s
1218 constant to be how many times each variable is subjected to trial moves
1219 within one pass through SA’s inner loop. Each variable is subjected to these
1220 n_s trials sequentially. Consequently, the value $n \times n_s$ becomes in-effect, their
1221 chain length. These authors do not attempt to equate their de-facto chain
1222 length definition with the number of possible points accessible in one move
1223 – and instead, simply recommend n_s be set to 20. In SA-MDAS, however,
1224 a move always consists of a possible step-change on each and every variable.
1225 Therefore, in SA-MDAS, n_s is the number of times that moves are made
1226 within one pass through SA’s inner loop.

1227 As in Corana et al. (1987), SA-MDAS recomputes each variable’s step
1228 length every pass through the outer loop. Except for initialization, step
1229 length updates in SA-MDAS use equations given in (Corana et al., 1987, p.
1230 267).

1231 The step length’s “varying criterion,” Corana et al. (1987) and the step
1232 lengths themselves need to be initialized. This is accomplished by first as-
1233 suming that the median is returned by the uniform random number generator
1234 on the unit interval, i.e., the value 0.5. Then, the initial median step length
1235 is initialized to be the width of the widest set of the n bound constraints
1236 divided by 50 – and then multiplied by this median value. The chain length
1237 is fixed at the value $10 \times n_s$ where $n_s = 3$.

1238 The continuous-variable scheme of Corana et al. (1987) for SA maintains
1239 an approximately 50% acceptance rate at every temperature, t . But this is

accomplished by progressively making the step length along each variable, smaller. Hence, as the temperature decreases, the chance that SA will break into a significantly more optimal subspace becomes small since, as the temperature decreases, a typical move will be close to the current point. Hence, at some temperature, the global search capability of SA will become practically nonexistent.

Stochastic objective functions

SA-MDAS can handle stochastic objective functions using a method developed by Bouttier and Gavra (2019). These authors define a “time” variable, t . To avoid confusion with this article’s notation for “temperature,” u is used here to refer to this variable. In the Bouttier and Gavra (2019) method, instead of evaluating the objective function once when a “score” evaluation is needed, the function is evaluated n_u times at the same point in the solution space. These n_u values are then averaged and returned as the score value at that point. The size of n_u increases as u (time) increases.

The value of u is updated every pass through the outer loop with $u = u + \zeta$ where ζ is a realization from the Exponential(1.0) distribution. Because the expected value of this distribution is 1.0, this update is, on average, adding the value 1.0 to u every pass through the outer loop. Addition of this stochastic term rather than the addition of the fixed value 1.0 to u every pass through the outer loop is necessary to allow the chain of SA-generated solutions to be modeled as a continuous-time Markov process. This is the model that is assumed in the proof of their method’s convergence.

Further, their method requires a function mapping u to n_u . One such function that is used by the authors in their numerical experiments is

$$n_u = f(u) = \lfloor u \rfloor \quad (5)$$

where $\lfloor . \rfloor$ is the floor function.

In Step (g) of the algorithm in Section 3.4, Bouttier and Gavra (2019) have the temperature, t decreased by some function of u such as $t = 1/u$. But doing so ignores the standard deviation of the objective function estimated after each pass through SA’s inner loop. Hence, SA-MDAS employs the Aarts and Korst (1989) algorithm to decrement t for both deterministic objective functions and for stochastic objective functions.

1272 *Inter-performer coupling*

1273 By executing its MPE Step, SA-MDAS couples the performers to each
1274 other by allowing them to always begin their respective chains at the current
1275 best solution that was found across all performers during the last outer loop
1276 iteration.

1277 *Message-passing overhead*

1278 Spreading tasks across a cluster of performers as is done in SA-MDAS is
1279 known to have some amount of *latency* (Pichetti et al., 2024). Here, such
1280 latency is viewed as a minor issue because the optimization problem’s ob-
1281 jective function, being composed of interacting agent/individual stochastic
1282 submodels, is computationally expensive to evaluate. Hence, most of the
1283 compute time needed to estimate the parameters of the political-ecological
1284 model will typically be taken by objective function evaluations rather than
1285 by inter-node messaging.

1286 To verify this hunch, an experiment was conducted using Bukin’s F4 func-
1287 tion. This function takes very little compute time. SA-MDAS was run on
1288 a WindowsTM laptop computer with 32 GB of memory running at 1.2 GHz.
1289 Doing so resulted in SA-MDAS requiring 1.62 seconds to compute 192K eval-
1290 uations of Bukin’s F4 function. SA-MDAS was next run on the TSCC to
1291 perform 1,400 evaluations of this same function using two performers com-
1292 municating with the impresario through a GigaSpace. Wall clock time for
1293 these evaluations was seven minutes. Almost all of this time was devoted to
1294 inter-node message-passing. These values suggest that a GigaSpaces imple-
1295 mentation of SA-MDAS requires about 0.3 seconds to complete a *round-trip*,
1296 i.e., the posting of a task to the GigaSpace, a performer down-loading the
1297 task, uploading the result, and the impresario taking the result off of the
1298 GigaSpace. Note that a round-trip does not include the objective function’s
1299 evaluation.

1300 Let x be the number of minutes needed to evaluate the objective func-
1301 tion. Assume a 100-node cluster computer is available. Then, the break-even
1302 function evaluation time can be estimated by solving for x in:

$$192000x = 192000x/100 + 192000(0.3/60) \quad (6)$$

1303 The left side of 6 is the time needed to compute 192K function evaluations
1304 on a single-processor computer, while the right side is the time needed to
1305 compute the same number of evaluations on a cluster computer running 100
1306 nodes in parallel. Equation 6 can be written as $0.99x = 0.3/60$, i.e., x is
1307 approximately equal to the roundtrip time. Hence, for expensive functions,
1308 cluster computing can speed-up black-box optimization problems even when
1309 round-trip times are as large as 0.3 seconds. And further, this speed-up
1310 increases as the objective function's evaluation time increases.

1311 Evaluating the political-ecological model's CA objective function in the
1312 example of Section 4, requires about 15 seconds. Hence, an optimization
1313 algorithm that scales on the increasing availability of cluster computer nodes,
1314 is currently, the only feasible way to statistically fit a large political-ecological
1315 model to data.

1316 *Comparisons with other optimization algorithms*

1317 The optimization problem of least sum-of-squares possesses a very smooth,
1318 unimodal objective function. Using only phase one (SA), SA-MDAS needed
1319 3,780 evaluations to solve a 27-variable least sum-of-squares problem. Whereas
1320 a Hooke and Jeeves algorithm (Haas, 2020) needed 1,725 evaluations, and a
1321 Random Search algorithm (Schumer and Steiglitz (1968)) needed 1,568 eval-
1322 uations. These latter two algorithms are local, nonstochastic, and do not
1323 scale well as neither can make use of more than one compute node.

1324 Similar to PACSA, SA-MDAS phase one mainly uses parallel processing
1325 to store the end result of many chains in order to increase the chance that it
1326 will find the global minimum point – not necessarily to speed up the solution
1327 time (Gonçalves-e-Silva et al., 2018). In other words, the focus of SA-MDAS
1328 phase one is to find the global minimum, not to speed up the solution. Even
1329 with this caveat, SA-MDAS phase one takes only about twice as long to solve
1330 a 27-variable least-squares problem as do two strictly local-search algorithms.

1331 SA performs global search through decisions to probabilistically accept
1332 uphill moves (worse objective function values) rather than delineating a par-
1333 titioning of the solution space first and then evaluating the function at some
1334 point in each partition as is done for example, in Jia et al. (2024). Such a
1335 partitioning-then-evaluation approach to global optimization results in many

1336 objective function evaluations regardless of whether they end up being uphill
1337 or downhill values. Further, there is an implicit assumption that all points
1338 within a partition have function values that are similar to the value at the
1339 single point actually evaluated in that partition.

1340 MDAS, being more focused on local search than SA, employs many per-
1341 formers to

- 1342 1. Perform limited global search (up to the m dimensions (variables) being
1343 searched simultaneously), and
- 1344 2. Produce a speedup from the sequential Hooke and Jeeves algorithm
1345 by evaluating the objective function at all m -dimensions-ahead search
1346 points simultaneously rather than sequentially.